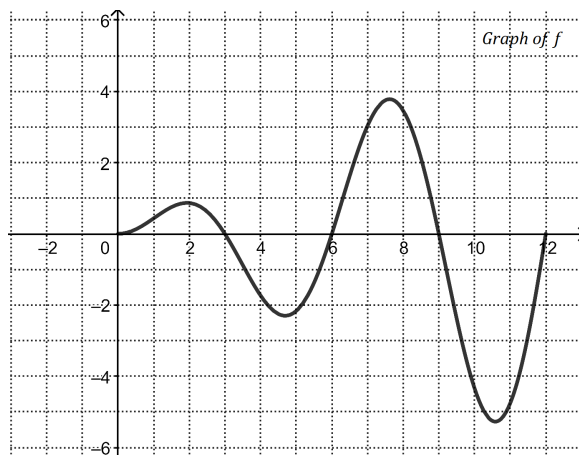


1. Suppose we are given the below data about  $f : [0, \frac{\pi}{4}] \rightarrow \mathbb{R}$ .

$f(0)$	$f(\frac{\pi}{4})$	$f(\frac{\pi}{2})$
0	$\frac{1}{\sqrt{2}}$	1

- (a) Use the part (c) to provide an approximation of  $\int_0^{\frac{\pi}{4}} f(x)dx$ .
  - (b) Suppose  $f(x) = \sin(x)$  then quantify the error in each approximation.
  - (c) Are their functions for which the approximation(s) will be exact ?
2. The graph of a function  $f(t)$  is shown. Use it to answer the following questions.



- (a) Using 1(c) provide an approximation of the **average value** of this function over the interval  $[4, 12]$ .
- (b) Can you provide a better approximation of the same using 1(c) ?