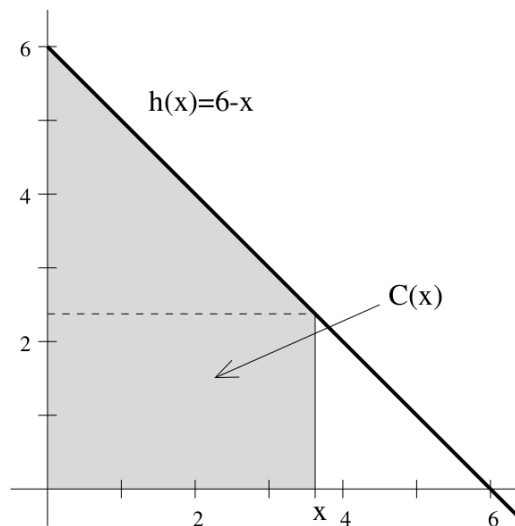


1. As described in figure, define  $C(x)$  to be the area bounded by the  $x$ -axis and the function  $h(x) = 6 - x$



between  $y$ -axis and the the vertical line at  $x$ , with  $x > 0$ .

- Find  $C(2)$ ,  $C(3) - C(1)$  and  $C(4)$ .
  - Find a formula for  $C(x)$  for general  $x > 0$  and  $C'(x)$ .
2. Define  $E(a)$  to be the area bounded by the  $x$ -axis and the function  $f(x) = e^x$  between the vertical line at  $x = 0$ , and the vertical line at  $x = a$ , with  $a > 0$ .
- Using a rough sketch, slice the area bounded by the  $x$ -axis and the function  $f(x) = e^x$  between the vertical line at  $x = 0$ , and the vertical line at  $x = 1$  into 4 pieces by drawing 3 evenly spaced vertical lines from the  $x$ -axis up to the curve.
  - Using the left side of each slice as the height, draw 4 rectangles on your graph. Find the areas of the 4 rectangles and add them up ( $\equiv U_1$ ).
  - Using the right side of each slice as the height, draw 4 rectangles on your graph. Find the areas of the 4 rectangles and add them up ( $\equiv L_1$ ).
  - Find the average of  $U_1$  and  $L_1$
  - Compare all the above answers with  $e - 1$  in your calculator.